

Razvoj softvera - Primeri, čas 7 - Polimorfizam

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p11_sablони.cpp

```
#include <iostream>
using namespace std;

// pocetni primer, upotreba makroa
#define max1(x,y) ((x) > (y) ? (x) : (y))

int main()
{
    cout << max1(1,2) << endl;
    cout << max1(2.45, 2.54) << endl;

    int a=2;
    // koliko ce biti a?
    cout << max1(a++,a--) << endl;
    cout << a << endl;
}
```

p12_sablони.cpp

```
#include <iostream>
using namespace std;

// zamena makroa inline funkcijom
// - jednako efikasno kao makro
// - bezbedna sintaksa
// - manja fleksibilnost - samo za jedan tip podataka
inline int max1( int x, int y )
{
    return x > y ? x : y;
}

int main()
{
    cout << max1(1,2) << endl;
    cout << max1(2.45, 2.54) << endl;

    int a=2;
    // koliko ce biti a?
    cout << max1(a++,a--) << endl;
}
```

```
    cout << a << endl;
}
```

p13_sablioni.cpp

```
#include <iostream>
using namespace std;

// zamena funkcije sablonom funkcije
// - jednako efikasno kao makro
// - bezbedna sintaksa
// - ista ili cak veca fleksibilnost
template <class T>
inline const T& max1( const T& x, const T& y )
{
    return x > y ? x : y;
}

int main()
{
    cout << max1(1,2) << endl;
    cout << max1(2.45, 2.54) << endl;

    // primer neispravnog implicitnog instanciranja
    // cout << max1(1, 2.5) << endl;
    // mora eksplicitno:
    cout << max1<double>(1, 2.5) << endl;
    cout << max1<char>( 'a', 53.2 ) << endl;

    int a=2;
    // koliko ce biti a?
    cout << max1(a++,a--) << endl;
    cout << a << endl;
}
```

p14_sablioni.cpp

```
#include <iostream>
#include <cstring>
using namespace std;

// zamena funkcije sablonom funkcije
// - jednako efikasno kao makro
// - bezbedna sintaksa
// - ista ili cak veca fleksibilnost
template <class T>
inline T max1( T x, T y )
{
    return x > y ? x : y;
}
```

```

// eksplicitna specijalizacija za const char*
template<>
inline const char* max1( const char* x, const char* y ) {
    cout << "poziv sablona" << endl;
    return strcmp(x,y)>0 ? x : y;
}

// naredna funkcija nije isto sto i prethodna, zato sto ona nije sablon
inline const char* max1( const char* x, const char* y ) {
    cout << "poziv funkcije" << endl;
    return x>y ? x : y;
}

// parametar sablona moze da bude i konstanta
// koja se vezuje u vreme prevodjenja
template<int N>
inline bool veceOd( int x )
{
    return x > N;
}

int main()
{
    cout << max1(1,2) << endl;
    cout << max1(2.45, 2.54) << endl;

    // primer neispravnog implicitnog instanciranja
    // cout << max1(1, 2.5) << endl;
    // mora eksplicitno:
    cout << max1<double>(1, 2.5) << endl;
    cout << max1<char>( 'a', 53.2 ) << endl;

    // ovde se poziva sablon za T=const char*
    cout << max1<>("aaa", "bbb") << endl;

    // ovde se poziva funkcija
    cout << max1("aaa", "bbb") << endl;

    // ovde se proverava da li je 10 vece od 5
    // 5 se vezuje u vreme prevodjenja, a 10 u vreme izvrshavanja
    // (u ovom slucaju se i 10 vezuje u vreme prevodjenja zbog 'inline')
    cout << veceOd<5>(10) << endl;
}

```

p21_sablони_klasа.cpp

```

#include <iostream>
using namespace std;

// primer jednostavne konkretne klase

```

```

class Tacka
{
public:
    int x,y,z;
    Tacka(int x0, int y0, int z0)
        : x(x0), y(y0), z(z0)
        {}
};

ostream& operator<<( ostream& ostr, const Tacka& t )
{
    ostr << "(" << t.x << "," << t.y << "," << t.z << ")";
    return ostr;
}

int main()
{
    Tacka t(1,2,3);
    cout << t << endl;
    cout << Tacka(1.2, 1.3, 1.4) << endl;
}

```

p22_sablioni_klasa.cpp

```

#include <iostream>
using namespace std;

// pravljenje dve jednostavne konkretne klase
// koje se razlikuju samo po tipu elemenata

class Tacka
{
public:
    int x,y,z;
    Tacka(int x0, int y0, int z0)
        : x(x0), y(y0), z(z0)
        {}
};

ostream& operator<<( ostream& ostr, const Tacka& t )
{
    ostr << "(" << t.x << "," << t.y << "," << t.z << ")";
    return ostr;
}

class TackaR
{
public:
    float x,y,z;
    TackaR(float x0, float y0, float z0)
        : x(x0), y(y0), z(z0)

```

```

    {}
};

ostream& operator<<( ostream& ostr, const TackaR& t )
{
    ostr << "(" << t.x << "," << t.y << "," << t.z << ")";
    return ostr;
}

int main()
{
    Tacka t(1,2,3);
    cout << t << endl;
    cout << Tacka(1.2, 1.3, 1.4) << endl;
    cout << TackaR(1.2, 1.3, 1.4) << endl;
}

```

p23_sablioni_klasa.cpp

```

#include <iostream>
using namespace std;

// uopstavanje razlicitih klasa jednim sablonom klase

template <class T>
class Tacka
{
public:
    T x,y,z;
    Tacka(T x0, T y0, T z0)
        : x(x0), y(y0), z(z0)
        {}
};

template <class T>
ostream& operator<<( ostream& ostr, const Tacka<T>& t )
{
    ostr << "(" << t.x << "," << t.y << "," << t.z << ")";
    return ostr;
}

int main()
{
    Tacka<int> t(1,2,3);
    cout << t << endl;
    cout << Tacka<int>(1.2, 1.3, 1.4) << endl;
    cout << Tacka<float>(1.2, 1.3, 1.4) << endl;
}

```

p24_sablioni_klasa.cpp

```

#include <iostream>
using namespace std;

// podrazumevane vrednosti parametara sablona

template <class T = int>
class Tacka
{
public:
    T x,y,z;
    Tacka(T x0, T y0, T z0)
        : x(x0), y(y0), z(z0)
        {}
};

template <class T>
ostream& operator<<( ostream& ostr, const Tacka<T>& t )
{
    ostr << "(" << t.x << "," << t.y << "," << t.z << ")";
    return ostr;
}

int main()
{
    Tacka<> t(1,2,3);
    cout << t << endl;
    cout << Tacka<>(1.2, 1.3, 1.4) << endl;
    cout << Tacka<float>(1.2, 1.3, 1.4) << endl;
}

```

p401_funkcionalni.cpp

```

#include <iostream>
#include <vector>

// prebrojavanje neparnih podataka u nizu, klasican pristup

using namespace std;

unsigned prebrojNeparne( const vector<int>& niz )
{
    unsigned n=0;
    for( int x : niz )
        if( x % 2 )
            n++;
    return n;
}

int main()
{
    vector<int> niz;

```

```

for( unsigned i=0; i<100; i++ )
    niz.push_back(i);

cout << prebrojNeparne(niz) << endl;

return 0;
}

```

p402_funkcionalni.cpp

```

#include <iostream>
#include <vector>

// izdvajanje uslova u funkciju

using namespace std;

bool neparan( int n )
{
    return n%2;
}

unsigned prebrojNeparne( const vector<int>& niz )
{
    unsigned n=0;
    for( int x : niz )
        if( neparan( x ) )
            n++;
    return n;
}

int main()
{
    vector<int> niz;
    for( unsigned i=0; i<100; i++ )
        niz.push_back(i);

    cout << prebrojNeparne(niz) << endl;

    return 0;
}

```

p403_funkcionalni.cpp

```

#include <iostream>
#include <vector>

// upotreba funkcijskog parametra

using namespace std;

```

```

bool neparan( int n )
{
    return n%2;
}

unsigned prebroj( const vector<int>& niz, bool(*uslov)(int) )
{
    unsigned n=0;
    for( int x : niz )
        if( uslov( x ))
            n++;
    return n;
}

int main()
{
    vector<int> niz;
    for( unsigned i=0; i<100; i++ )
        niz.push_back(i);

    cout << prebroj(niz,neparan) << endl;

    return 0;
}

```

p404_funkcionalni.cpp

```

#include <iostream>
#include <vector>

// uopstavanje tipova pomocu sablona

using namespace std;

bool neparan( int n )
{
    return n%2;
}

template<typename T>
unsigned prebroj( const vector<T>& niz, bool(*uslov)(T) )
{
    unsigned n=0;
    for( const T& x : niz )
        if( uslov( x ))
            n++;
    return n;
}

int main()
{

```



```

vector<int> niz;
for( unsigned i=0; i<100; i++ )
    niz.push_back(i);

cout << prebroj(niz,neparan) << endl;

return 0;
}

```

p405_funkcionalni.cpp

```

#include <iostream>
#include <vector>

// uopstavanje obilaska kolekcije pomocu iteratora
// ovaj korak je nepotreban kada se koristi ranged-for
using namespace std;

bool neparan( int n )
{
    return n%2;
}

template<typename T>
unsigned prebroj( const vector<T>& niz, bool(*uslov)(T) )
{
    unsigned n=0;
    for( const T& x : niz )
        if( uslov( x ) )
            n++;
    return n;
}

int main()
{
    vector<int> niz;
    for( unsigned i=0; i<100; i++ )
        niz.push_back(i);

    cout << prebroj(niz,neparan) << endl;

    return 0;
}

```

p406_funkcionalni.cpp

```

#include <iostream>
#include <vector>
#include <list>

```

```

// uopstavanje tipa kolekcije, zato sto se i druge kolekcije
// obilaze na isti nacin pomocu iteratora
// i ovaj korak je nepotreban kada se koristi ranged-for
using namespace std;

bool neparan( int n )
{
    return n%2;
}

template<typename T, typename TK>
unsigned prebroj( const TK& kolekcija , bool(*uslov)(T) )
{
    unsigned n=0;
    for( const T& x : kolekcija )
        if( uslov( x ) )
            n++;

    // ako se koriste iteratori, mora ovako:
    // kljucna rec 'typename' je nephodna po standardu da bi se
    // prevodiocu naglasilo da je TK::const_iterator ime tipa
// typename TK::const_iterator
//     i = kolekcija.begin(),
//     e = kolekcija.end();
// for( ; i!=e; i++ )
//     if( uslov( *i ) )
//         n++;

    return n;
}

int main()
{
    // vector<int> niz;
    list<int> niz;
    for( unsigned i=0; i<100; i++ )
        niz.push_back(i);

    cout << prebroj(niz,neparan) << endl;

    return 0;
}

```

p407_funkcionalni.cpp

```

#include <iostream>
#include <vector>
#include <list>

// izdvajanje obilaska pomocu iteratora
// veliki deo standardne biblioteke pociva na tom pristupu

```

```

using namespace std;

bool neparan( int n )
{
    return n%2;
}

template<typename T, typename Iterator>
unsigned prebroj( Iterator beg, Iterator end, bool(*uslov)(T) )
{
    unsigned n=0;
    for( Iterator i=beg; i!=end; i++ )
        if( uslov( *i ) )
            n++;
    return n;
}

template<typename T, typename TK>
unsigned prebroj( const TK& kolekcija , bool(*uslov)(T) )
{
    return prebroj( kolekcija.begin(), kolekcija.end(), uslov );
}

int main()
{
    vector<int> niz;
    for( unsigned i=0; i<100; i++ )
        niz.push_back(i);

    cout << prebroj(niz,neparan) << endl;
    cout << prebroj(niz.begin(), niz.end(),neparan) << endl;
    cout << prebroj(niz.begin()+20, niz.begin()+35,neparan) << endl;

    // ovo ne moze sa svim kolekcijama, jer ne mogu svi iteratori da idu unazad
    cout << prebroj(niz.begin()+20, niz.end()-25,neparan) << endl;

    return 0;
}

```

p408_funkcionalni.cpp

```

#include <iostream>
#include <vector>
#include <list>

// parametrizujemo tip funkcije sablonom
// tj. parametarskim tipom Predikat
// "Predikat" je unarna logicka funkcija

using namespace std;

bool neparan( int n )

```

```

{
    return n%2;
}

template<typename Iterator, typename Predikat>
unsigned prebroj( Iterator beg, Iterator end, Predikat uslov )
{
    unsigned n=0;
    for( Iterator i=beg; i!=end; i++ )
        if( uslov( *i ) )
            n++;
    return n;
}

template<typename TK, typename Predikat>
unsigned prebroj( const TK& kolekcija , Predikat uslov )
{
    return prebroj( kolekcija.begin(), kolekcija.end(), uslov );
}

int main()
{
    vector<int> niz;
    for( unsigned i=0; i<100; i++ )
        niz.push_back(i);

    cout << prebroj(niz,neparan) << endl;
    cout << prebroj(niz.begin(), niz.end(),neparan) << endl;
    cout << prebroj(niz.begin()+20, niz.begin()+35,neparan) << endl;

    // ovo ne moze sa svim kolekcijama, jer ne mogu svi iteratori da idu unazad
    cout << prebroj(niz.begin()+20, niz.end()-25,neparan) << endl;

    return 0;
}

```

p409_funkcionalni.cpp

```

#include <iostream>
#include <vector>

// dodajemo novu funkciju koju koristimo kao predikat

using namespace std;

bool neparan( int n )
{
    return n%2;
}

bool veciOd5( int n )
{

```

```

    return n > 5;
}

bool veci0d3( double n )
{
    return n > 5;
}

template<typename Iterator, typename Predikat>
unsigned prebroj( Iterator beg, Iterator end, Predikat uslov )
{
    unsigned n=0;
    for( Iterator i=beg; i!=end; i++ )
        if( uslov( *i ) )
            n++;
    return n;
}

template<typename TK, typename Predikat>
unsigned prebroj( const TK& kolekcija, Predikat uslov )
{
    return prebroj( kolekcija.begin(), kolekcija.end(), uslov );
}

int main()
{
    vector<int> niz;
    for( unsigned i=0; i<100; i++ )
        niz.push_back(i);

    cout << prebroj(niz,neparan) << endl;
    cout << prebroj(niz.begin(), niz.end(),neparan) << endl;
    cout << prebroj(niz.begin()+20, niz.begin()+35,neparan) << endl;

    cout << prebroj(niz,veci0d5) << endl;
    cout << prebroj(niz.begin(), niz.end(),veci0d5) << endl;
    cout << prebroj(niz.begin()+20, niz.begin()+35,veci0d5) << endl;

    // Primetimo da ovde mozemo da koristimo i funkciju koja ne ocekuje ceo broj.
    // To ne bi moglo da je "uslov" ostao sa fiksnim tipom.
    cout << prebroj(niz,veci0d3) << endl;

    return 0;
}

```

p410_funkcionalni.cpp

```

#include <iostream>
#include <vector>

// Dodajemo i koristimo funkcional
// "Funkcional" je objekat (klasa) koja moze da se koristi

```

```

// kao funkcija, tj. ima definisan operator().
// Ovaj operator moze da postoji u razlicitim verzijama,
// za razlicite brojeve i tipove argumenata.

using namespace std;

bool neparan( int n )
{
    return n%2;
}

bool veciOd5( int n )
{
    return n > 5;
}

class Neparan
{
public:
    bool operator()( int n )
        { return n%2; }
};

template<typename Iterator, typename Predikat>
unsigned prebroj( Iterator beg, Iterator end, Predikat uslov )
{
    unsigned n=0;
    for( Iterator i=beg; i!=end; i++ )
        if( uslov( *i ) )
            n++;
    return n;
}

template<typename TK, typename Predikat>
unsigned prebroj( const TK& kolekcija, Predikat uslov )
{
    return prebroj( kolekcija.begin(), kolekcija.end(), uslov );
}

int main()
{
    vector<int> niz;
    for( unsigned i=0; i<100; i++ )
        niz.push_back(i);

    cout << prebroj(niz,neparan) << endl;
    cout << prebroj(niz.begin(), niz.end(),neparan) << endl;
    cout << prebroj(niz.begin()+20, niz.begin()+35,neparan) << endl;

    cout << prebroj(niz,veciOd5) << endl;
    cout << prebroj(niz.begin(), niz.end(),veciOd5) << endl;
    cout << prebroj(niz.begin()+20, niz.begin()+35,veciOd5) << endl;

    // koristimo objekat funkcional

```

```

Neparan nep;
cout << prebroj(niz,nep) << endl;
// koristimo privremeni objekat funkcional
cout << prebroj(niz.begin(), niz.end(), Neparan() ) << endl;
cout << prebroj(niz.begin()+20, niz.begin()+35, Neparan()) << endl;

return 0;
}

```

p411_funkcionalni.cpp

```

#include <iostream>
#include <vector>

// Dodajemo parametrizovan funkcional.

using namespace std;

bool neparan( int n )
{
    return n%2;
}

bool veciOd5( int n )
{
    return n > 5;
}

class Neparan
{
public:
    bool operator()( int n )
        { return n%2; }
};

class VeciOd
{
public:
    VeciOd( int n )
        : _N(n)
    {}

    bool operator()( int n )
        { return n > _N; }

private:
    int _N;
};

template<typename Iterator, typename Predikat>
unsigned prebroj( Iterator beg, Iterator end, Predikat uslov )
{

```

```

    unsigned n=0;
    for( Iterator i=beg; i!=end; i++ )
        if( uslov( *i ) )
            n++;
    return n;
}

template<typename TK, typename Predikat>
unsigned prebroj( const TK& kolekcija, Predikat uslov )
{
    return prebroj( kolekcija.begin(), kolekcija.end(), uslov );
}

int main()
{
    vector<int> niz;
    for( unsigned i=0; i<100; i++ )
        niz.push_back(i);

    cout << prebroj(niz,neparan) << endl;
    cout << prebroj(niz,veci0d5) << endl;
    cout << prebroj(niz,Neparan()) << endl;

    cout << prebroj(niz,Veci0d(10)) << endl;

    for( int i=0; i<100; i+=5 )
        cout << i << " : " << prebroj(niz,Veci0d(i)) << endl;

    return 0;
}

```

p412_funkcionalni.cpp

```

#include <iostream>
#include <vector>

// Ako hocemo da funkciju parametrizujemo samo staticki
// (tj. u vreme prevodjenja)
// onda umesto funkcionala mozemo da koristimo sablon.

using namespace std;

bool neparan( int n )
{
    return n%2;
}

bool veci0d5( int n )
{
    return n > 5;
}

```



```

class Neparan
{
public:
    bool operator()( int n )
        { return n%2; }
};

class VeciOd
{
public:
    VeciOd( int n )
        : _N(n)
        {}

    bool operator()( int n )
        { return n > _N; }

private:
    int _N;
};

template<int n>
bool veciOd( int x )
{
    return x > n;
}

template<typename Iterator, typename Predikat>
unsigned prebroj( Iterator beg, Iterator end, Predikat uslov )
{
    unsigned n=0;
    for( Iterator i=beg; i!=end; i++ )
        if( uslov( *i ) )
            n++;
    return n;
}

template<typename TK, typename Predikat>
unsigned prebroj( const TK& kolekcija, Predikat uslov )
{
    return prebroj( kolekcija.begin(), kolekcija.end(), uslov );
}

int main()
{
    vector<int> niz;
    for( unsigned i=0; i<100; i++ )
        niz.push_back(i);

    cout << prebroj(niz,neparan) << endl;
    cout << prebroj(niz,veciOd5) << endl;
    cout << prebroj(niz,Neparan()) << endl;

    cout << prebroj(niz,veciOd<5>) << endl;
}

```

```

for( int i=0; i<100; i+=5 )
    cout << i << " : " << prebroj(niz,VeciOd(i)) << endl;

return 0;
}

```

p413_funkcionalni.cpp

```

#include <iostream>
#include <vector>

// Funkcionalni su problematicni, zato sto se pisu udaljeno od mesta
// na kome se koriste, cak i onda kada se trivijalno definisu i kada
// smo sigurni da ih nikada vise necemo koristiti.
// Zbog toga C++ 11 uvodi pojednostavljenu "inline" sintaksu funkcionala,
// koja omogucava njihovo pisanje na mestu upotrebe, a prevod je prakticno
// ekvivalentan. To su tzv. "lambda funkcije".
// (mora da se prevodi za C++11)

using namespace std;

bool neparan( int n )
{
    return n%2;
}

bool veciOd5( int n )
{
    return n > 5;
}

class Neparan
{
public:
    bool operator()( int n )
        { return n%2; }
};

class VeciOd
{
public:
    VeciOd( int n )
        : _N(n)
    {}

    bool operator()( int n )
        { return n > _N; }

private:
    int _N;
};

```

```

template<int n>
bool veci0d( int x )
{
    return x > n;
}

template<typename Iterator, typename Predikat>
unsigned prebroj( Iterator beg, Iterator end, Predikat uslov )
{
    unsigned n=0;
    for( Iterator i=beg; i!=end; i++ )
        if( uslov( *i ) )
            n++;
    return n;
}

template<typename TK, typename Predikat>
unsigned prebroj( const TK& kolekcija, Predikat uslov )
{
    return prebroj( kolekcija.begin(), kolekcija.end(), uslov );
}

int main()
{
    vector<int> niz;
    for( unsigned i=0; i<100; i++ )
        niz.push_back(i);

    cout << prebroj(niz,neparan) << endl;
    cout << prebroj(niz,veci0d5) << endl;
    cout << prebroj(niz,Neparan()) << endl;

    cout << prebroj(niz,veci0d<5>) << endl;

    for( int i=0; i<100; i+=5 )
        cout << i << " : " << prebroj(niz,Veci0d(i)) << endl;

    // Ako je u pitanju jednostavna funkcija, tako se i prevodi.
    // Ovaj primer je ekvivalentan funkciji "neparan".
    //     [] - pocetak funkcije, ime nije potrebno zato sto je necemo drugde
koristiti
    //     (int n) - argumenti funkcije
    //     {...} - telo funkcije
    cout << prebroj( niz, [](int n){ return n%2; }) << endl;

    // Ako je u pitanju nesto slozenije, pa zelimo da funkciji prenesemo neke
    // promenljive koje su vidljive na mestu definisanja, onda je zapravo u pitanju
    // funkcional.
    // Ovaj primer je ekvivalentan funkcionalu "Veci0d".
    // [i] - naglasava da funkcional cuva parametar "i"
    //     kao da smo napisali:
    //     class Veci0d {
    //         int i;

```

```

//      VeciOd(int _i) : i(_i) {}
//      ...
//      }
//      i zatim napravili objekat sa "VeciOd(i)"
for( int i=0; i<100; i+=5 )
    cout << i << " : "
        << prebroj( niz, [i](int n){ return n>i; } ) << endl;

return 0;
}

```

p414_funkcionalni.cpp

```

#include <iostream>
#include <vector>

// Cesto imamo na raspolaganju funkciju koja je binarna
// a zelimo da je upotrebimo za definisanje unarne funkcije.
// Na primer, ako imamo "veciOd(x,y)" i zelimo da fiksiramo "y".
// Osim lambda funkcijama, to moze da se uradi i posebnim funkcionalom,
// koji 'pamti' i funkciju i argument.

using namespace std;

bool veciOd( int n, int m )
{
    return n > m;
}

// Funkcional Bind_2_2 pamti binarnu funkciju i njen 2. argument
template<typename Fn, typename T>
class Bind_2_2
{
public:
    Bind_2_2( Fn fn, T arg2 )
        : _Fn(fn), _Arg2(arg2)
    {}

    bool operator()( T n )
        { return _Fn(n, _Arg2); }

private:
    Fn _Fn;
    T _Arg2;
};

// Pravljenje sablonskog funkcionala zahteva eksplicitno navodjenje tipa
// na primer:
//      Bind_2_2<bool (*)(int,int),int>(veciOd,5)
// sto bas i nije mnogo zgodno za upotrebu,
// pa se zato pravi pomocni sablon funkcije, koji automatski raspoznaje
// upotrebljene tipove

```

```

template<typename Fn, typename T>
Bind_2_2<Fn,T> bind_2_2( Fn fn, T arg2 )
{
    return Bind_2_2<Fn,T>( fn, arg2 );
}

template<typename Iterator, typename Predikat>
unsigned prebroj( Iterator beg, Iterator end, Predikat uslov )
{
    unsigned n=0;
    for( Iterator i=beg; i!=end; i++ )
        if( uslov( *i ) )
            n++;
    return n;
}

template<typename TK, typename Predikat>
unsigned prebroj( const TK& kolekcija, Predikat uslov )
{
    return prebroj( kolekcija.begin(), kolekcija.end(), uslov );
}

int main()
{
    vector<int> niz;
    for( unsigned i=0; i<100; i++ )
        niz.push_back(i);

    cout << prebroj(niz, Bind_2_2<bool(*)>(int,int),int>(veci0d,17)) << endl;
    cout << prebroj(niz, bind_2_2(veci0d,17)) << endl;
    cout << prebroj(niz, bind_2_2([](int x,int y){return x>y;},17)) << endl;

    // Standardna biblioteka sadrzi napredniju verziju
    // funkcionala "bind", koja omogucava da se argumentom opise
    // koji se argument vezuje.

    return 0;
}

```

p61.niz.cpp

```

#include <iostream>
#include <vector>
#include <stdexcept>

using namespace std;

//-----
// niz sa proveravanjem opsega

template<typename T>
class Niz : public vector<T>

```

```

{
public:
    Niz()
        : vector<T>()
    {}

    Niz( unsigned int sz )
        : vector<T>( sz )
    {}

    T& operator[]( unsigned i )
    {
        if( i >= vector<T>::size() )
            throw out_of_range("Indeks van opsega");
        return vector<T>::operator[](i);
    }

    const T& operator[]( unsigned i ) const
    {
        if( i >= vector<T>::size() )
            throw out_of_range("Indeks van opsega");
        return vector<T>::operator[](i);
    }
};

//-----
int main()
{
    try {
        Niz<int> niz(20);

        for( unsigned i=0; i<niz.size(); i++ )
            niz[i] = i*i;
        for( unsigned i=0; i<=niz.size(); i++ )
            cout << i << " : " << niz[i] << endl;

    }catch( exception& e ){
        cerr << "*** GRESKA: " << e.what() << endl;
    }

    return 0;
}

```

p62.niz.cpp

```

#include <iostream>
#include <vector>
#include <stdexcept>

using namespace std;

// nizovi sa i bez provere indeksa

```

```

//-----
class ProveraIndeksa {
public:
    static void Provera( unsigned indeks, unsigned opseg ){
        if( indeks >= opseg )
            throw out_of_range("Indeks van opsega");
    }
};

class BezProvereIndeksa{
public:
    static void Provera( unsigned indeks, unsigned opseg ){ }
};

//-----
template<typename T,typename ProveravacIndeksa>
class Niz : public vector<T>
{
public:
    Niz( unsigned n )
        : vector<T>(n)
        {}

    T& operator[]( unsigned i )
    {
        ProveravacIndeksa::Provera( i, vector<T>::size() );
        return vector<T>::operator[](i);
    }

    const T& operator[]( unsigned i ) const
    {
        ProveravacIndeksa::Provera( i, vector<T>::size() );
        return vector<T>::operator[](i);
    }
};

//-----
int main()
{
    try {
        Niz<int,ProveraIndeksa> niz(10);
        for( unsigned i=0; i<niz.size(); i++ )
            niz[i] = i*i;
        for( unsigned i=0; i<=niz.size(); i++ )
            cout << i << " : " << niz[i] << endl;

        cout << niz[9999999] << endl;

    }catch( exception& e ){
        cerr << "*** GRESKA: " << e.what() << endl;
    }
}

```

```
    return 0;
}
```

p71.matrica.cpp

```
#include <iostream>
#include <vector>
#include <stdexcept>

using namespace std;

// nizovi i matrice sa proverom indeksa
// 'matrice' sa vecim brojem dimenzija

//-----
class ProveraIndeksa {
public:
    static void Provera( unsigned indeks, unsigned opseg ){
        if( indeks >= opseg )
            throw out_of_range("Indeks van opsega");
    }
};

class BezProvereIndeksa{
public:
    static void Provera( unsigned indeks, unsigned opseg ){ }
};

//-----
template<typename T,typename ProveravacIndeksa>
class Niz : public vector<T>
{
public:
    T& operator[]( unsigned i )
    {
        ProveravacIndeksa::Provera( i, vector<T>::size() );
        return vector<T>::operator[](i);
    }

    const T& operator[]( unsigned i ) const
    {
        ProveravacIndeksa::Provera( i, vector<T>::size() );
        return vector<T>::operator[](i);
    }
};

//-----
template<typename T, unsigned Dim, typename ProveravacIndeksa>
class Matrica
{
public:
    typedef Matrica<T,Dim-1,ProveravacIndeksa> tElementa;
```



```

Matrica()
{}

Matrica( unsigned dims[] ) {
    PostaviVelicinu( dims );
}

Matrica(unsigned d1,
        unsigned d2=0,
        unsigned d3=0,
        unsigned d4=0,
        unsigned d5=0,
        unsigned d6=0,
        unsigned d7=0,
        unsigned d8=0
        )
{
    unsigned d[] = { d1, d2, d3, d4, d5, d6, d7, d8 };
    PostaviVelicinu(d);
}

void PostaviVelicinu( unsigned dims[] ) {
    _Elementi.resize(dims[0]);
    for( unsigned i=0; i<dims[0]; i++ )
        _Elementi[i].PostaviVelicinu(dims+1);
}

tElementa& operator[]( unsigned d1 ) {
    return _Elementi[d1];
}

const tElementa& operator[]( unsigned d1 ) const {
    return _Elementi[d1];
}

unsigned size( unsigned d ) const {
    if( d==1 )
        return _Elementi.size();
    else
        return _Elementi[0].size(d-1);
}

private:
    Niz<tElementa,ProveravacIndeksa> _Elementi;
};

//-----
template<typename T, typename ProveravacIndeksa>
class Matrica<T,1,ProveravacIndeksa>
{
public:
    Matrica()
    {}

```

```

void PostaviVelicinu( unsigned dims[] ) {
    _Elementi.resize(dims[0]);
}

T& operator[]( unsigned d1 ) {
    return _Elementi[d1];
}

const T& operator[]( unsigned d1 ) const {
    return _Elementi[d1];
}

unsigned size( unsigned d ) const {
    ProveravacIndeksa::Provera( d-1, 1 );
    return _Elementi.size();
}

private:
    Niz<T,ProveravacIndeksa> _Elementi;
};

//-----
int main()
{
    try {
        Matrica<int,2,ProveraIndeksa> m(10,5);
        for(unsigned i=0;i<m.size(1);i++)
            for(unsigned j=0; j<m.size(2); j++ )
                m[i][j] = i*100 + j;

        for(unsigned i=0;i<m.size(1);i++){
            for(unsigned j=0; j<m.size(2); j++ )
                cout << m[i][j] << ' ';
            cout << endl;
        }
        cout << endl;

        cout << m[5][10] << endl;

    }catch( exception& e ){
        cerr << "*** GRESKA: " << e.what() << endl;
    }

    return 0;
}

```

p72.matrica.cpp

```

#include <iostream>
#include <vector>

```

```

#include <stdexcept>

using namespace std;

// nizovi i matrice sa proverom indeksa
// 'matrice' sa vecim brojem dimenzija

//-----
class ProveraIndeksa {
public:
    static void Provera( unsigned indeks, unsigned opseg ){
        if( indeks >= opseg )
            throw out_of_range("Indeks van opsega");
    }
};

class BezProvereIndeksa{
public:
    static void Provera( unsigned indeks, unsigned opseg ){
};

//-----
template<typename T,typename ProveravacIndeksa>
class Niz : public vector<T>
{
public:
    T& operator[]( unsigned i )
    {
        ProveravacIndeksa::Provera( i, size() );
        return vector<T>::operator[](i);
    }

    const T& operator[]( unsigned i ) const
    {
        ProveravacIndeksa::Provera( i, size() );
        return vector<T>::operator[](i);
    }

    using vector<T>::size;
};

//-----
template<typename T, unsigned Dim, typename ProveravacIndeksa>
class Matrica
{
public:
    typedef Matrica<T,Dim-1,ProveravacIndeksa> tElementa;

    Matrica()
    {}

    Matrica( unsigned dims[] ) {
        PostaviVelicinu( dims );
    }
};

```

```

Matrica(unsigned d1,
        unsigned d2=0,
        unsigned d3=0,
        unsigned d4=0,
        unsigned d5=0,
        unsigned d6=0,
        unsigned d7=0,
        unsigned d8=0
        )
{
    ProveravacIndeksa::Provera( Dim-1, 8 );
    unsigned d[] = { d1, d2, d3, d4, d5, d6, d7, d8 };
    PostaviVelicinu(d);
}

void PostaviVelicinu( unsigned dims[] ) {
    _Elementi.resize(dims[0]);
    for( unsigned i=0; i<dims[0]; i++ )
        _Elementi[i].PostaviVelicinu(dims+1);
}

tElementa& operator[]( unsigned d1 ) {
    return _Elementi[d1];
}

const tElementa& operator[]( unsigned d1 ) const {
    return _Elementi[d1];
}

unsigned size( unsigned d ) const {
    if( d==1 )
        return _Elementi.size();
    else
        return _Elementi[0].size(d-1);
}

private:
    Niz<tElementa,ProveravacIndeksa> _Elementi;
};

//-----
template<typename T, typename ProveravacIndeksa>
class Matrica<T,1,ProveravacIndeksa>
{
public:
    Matrica()
    {}

    void PostaviVelicinu( unsigned dims[] ) {
        _Elementi.resize(dims[0]);
    }

    T& operator[]( unsigned d1 ) {

```

```

    return _Elementi[d1];
}

const T& operator[]( unsigned d1 ) const {
    return _Elementi[d1];
}

unsigned size( unsigned d ) const {
    ProveravacIndeksa::Provera( d-1, 1 );
    return _Elementi.size();
}

private:
    Niz<T,ProveravacIndeksa> _Elementi;
};

//-----
int main()
{
    try {
        Matrica<int,3,ProveraIndeksa> m(10,2,5);
        cout << m.size(1) << endl;
        cout << m.size(2) << endl;
        cout << m.size(3) << endl;
        cout << endl;

    }catch( exception& e ){
        cerr << "*** GRESKA: " << e.what() << endl;
    }

    return 0;
}

```

p73.matrica.cpp

```

#include <iostream>
#include <vector>
#include <stdexcept>

using namespace std;

// dodati testovi

//-----
class ProveraIndeksa {
public:
    static void Provera( unsigned indeks, unsigned opseg ){
        if( indeks >= opseg )
            throw out_of_range("Indeks van opsega");
    }
};

```

```

class BezProvereIndeksa{
public:
    static void Provera( unsigned indeks, unsigned opseg ){}
};

//-----
template<typename T,typename ProveravacIndeksa>
class Niz : public vector<T>
{
public:
    T& operator[]( unsigned i )
    {
        ProveravacIndeksa::Provera( i, size() );
        return vector<T>::operator[](i);
    }

    const T& operator[]( unsigned i ) const
    {
        ProveravacIndeksa::Provera( i, size() );
        return vector<T>::operator[](i);
    }

    using vector<T>::size;
};

//-----
template<typename T, unsigned Dim, typename ProveravacIndeksa>
class Matrica
{
public:
    typedef Matrica<T,Dim-1,ProveravacIndeksa> tElementa;

    Matrica()
    {}

    Matrica( unsigned dims[] ) {
        PostaviVelicinu( dims );
    }

    Matrica(unsigned d1,
            unsigned d2=0,
            unsigned d3=0,
            unsigned d4=0,
            unsigned d5=0,
            unsigned d6=0,
            unsigned d7=0,
            unsigned d8=0
            )
    {
        ProveravacIndeksa::Provera( Dim-1, 8 );
        unsigned d[] = { d1, d2, d3, d4, d5, d6, d7, d8 };
        PostaviVelicinu(d);
    }
}

```

```

void PostaviVelicinu( unsigned dims[] ) {
    _Elementi.resize(dims[0]);
    for( unsigned i=0; i<dims[0]; i++ )
        _Elementi[i].PostaviVelicinu(dims+1);
}

tElementa& operator[]( unsigned d1 ) {
    return _Elementi[d1];
}

const tElementa& operator[]( unsigned d1 ) const {
    return _Elementi[d1];
}

unsigned size( unsigned d ) const {
    if( d==1 )
        return _Elementi.size();
    else
        return _Elementi[0].size(d-1);
}

private:
    Niz<tElementa,ProveravacIndeksa> _Elementi;
};

//-----
template<typename T, typename ProveravacIndeksa>
class Matrica<T,1,ProveravacIndeksa>
{
public:
    Matrica()
    {}

    void PostaviVelicinu( unsigned dims[] ) {
        _Elementi.resize(dims[0]);
    }

    T& operator[]( unsigned d1 ) {
        return _Elementi[d1];
    }

    const T& operator[]( unsigned d1 ) const {
        return _Elementi[d1];
    }

    unsigned size( unsigned d ) const {
        ProveravacIndeksa::Provera( d-1, 1 );
        return _Elementi.size();
    }

private:
    Niz<T,ProveravacIndeksa> _Elementi;
};

```

```

//-----
void test2()
{
    Matrica<int,2,ProveraIndeksa> m(10,5);
    for(unsigned i=0;i<m.size(1);i++)
        for(unsigned j=0; j<m.size(2); j++ )
            m[i][j] = i*100 + j;

    for(unsigned i=0;i<m.size(1);i++){
        for(unsigned j=0; j<m.size(2); j++ )
            cout << m[i][j] << ' ';
        cout << endl;
    }
}

void test3()
{
    Matrica<int,3,ProveraIndeksa> m(4,5,6);
    for(unsigned i=0;i<m.size(1);i++)
        for(unsigned j=0; j<m.size(2); j++ )
            for(unsigned k=0; k<m.size(3); k++ )
                m[i][j][k] = (i+1)*100 + (j+1)*10 + (k+1);

    for(unsigned i=0;i<m.size(1);i++){
        for(unsigned j=0; j<m.size(2); j++ ){
            for(unsigned k=0; k<m.size(3); k++ )
                cout << m[i][j][k] << ' ';
            cout << endl;
        }
        cout << "-----" << endl;
    }
}

void test3a()
{
    Matrica<int,3,ProveraIndeksa> m(4,5,6);
    for(unsigned i=0;i<m.size(1);i++){
        Matrica<int,2,ProveraIndeksa> m2(5,6);
        for(unsigned k=0;k<m2.size(1);k++)
            for(unsigned j=0; j<m2.size(2); j++ )
                m2[k][j] = (i+1)*1000 + k*100 + j;
        m[i] = m2;
    }

    for(unsigned i=0;i<m.size(1);i++){
        for(unsigned j=0; j<m.size(2); j++ ){
            for(unsigned k=0; k<m.size(3); k++ )
                cout << m[i][j][k] << ' ';
            cout << endl;
        }
        cout << "-----" << endl;
    }
}

```



```

int main()
{
    try {
        test2();
        test3();
        test3a();
    }catch( exception& e ){
        cerr << "*** GRESKA: " << e.what() << endl;
    }

    return 0;
}

```

p74.matrica.cpp

```

#include <iostream>
#include <vector>
#include <stdexcept>

using namespace std;

// dodati testovi

//-----
class ProveraIndeksa {
public:
    static void Provera( unsigned indeks, unsigned opseg ){
        if( indeks >= opseg )
            throw out_of_range("Indeks van opsega");
    }
};

class BezProvereIndeksa{
public:
    static void Provera( unsigned indeks, unsigned opseg ){
};

//-----
template<typename T,typename ProveravacIndeksa>
class Niz : public vector<T>
{
public:
    T& operator[]( unsigned i )
    {
        ProveravacIndeksa::Provera( i, size() );
        return vector<T>::operator[](i);
    }

    const T& operator[]( unsigned i ) const
    {

```

```

        ProveravacIndeksa::Provera( i, size() );
        return vector<T>::operator[](i);
    }

    using vector<T>::size;
};

//-----
template<typename T, unsigned Dim, typename ProveravacIndeksa>
class Matrica
{
public:
    typedef Matrica<T,Dim-1,ProveravacIndeksa> tElementa;

    Matrica()
    {}

    template<typename... Args>
    Matrica( unsigned n, Args... args )
    {
        PostaviVelicinu( n, args... );
    }

    template<typename... Args>
    void PostaviVelicinu( unsigned dim, Args... args ) {
        _Elementi.resize( dim );
        for( auto& m: _Elementi )
            m.PostaviVelicinu( args... );
    }

    tElementa& operator[]( unsigned d1 ) {
        return _Elementi[d1];
    }

    const tElementa& operator[]( unsigned d1 ) const {
        return _Elementi[d1];
    }

    unsigned size( unsigned d ) const {
        if( d==1 )
            return _Elementi.size();
        else
            return _Elementi[0].size(d-1);
    }

private:
    Niz<tElementa,ProveravacIndeksa> _Elementi;
};

//-----
template<typename T, typename ProveravacIndeksa>
class Matrica<T,1,ProveravacIndeksa>
{
public:

```

```

Matrica()
{}

Matrica( unsigned n )
{
    PostaviVelicinu( n );
}

void PostaviVelicinu( unsigned dim ) {
    _Elementi.resize(dim);
}

T& operator[]( unsigned d1 ) {
    return _Elementi[d1];
}

const T& operator[]( unsigned d1 ) const {
    return _Elementi[d1];
}

unsigned size( unsigned d ) const {
    ProveravacIndeksa::Provera( d-1, 1 );
    return _Elementi.size();
}

private:
    Niz<T,ProveravacIndeksa> _Elementi;
};

//-----
void test2()
{
    Matrica<int,2,ProveraIndeksa> m(10,5);
    for(unsigned i=0;i<m.size(1);i++)
        for(unsigned j=0; j<m.size(2); j++ )
            m[i][j] = i*100 + j;

    for(unsigned i=0;i<m.size(1);i++){
        for(unsigned j=0; j<m.size(2); j++ )
            cout << m[i][j] << ' ';
        cout << endl;
    }
}

void test3()
{
    Matrica<int,3,ProveraIndeksa> m(4,5,6);
    for(unsigned i=0;i<m.size(1);i++)
        for(unsigned j=0; j<m.size(2); j++ )
            for(unsigned k=0; k<m.size(3); k++ )
                m[i][j][k] = (i+1)*100 + (j+1)*10 + (k+1);

    for(unsigned i=0;i<m.size(1);i++){
        for(unsigned j=0; j<m.size(2); j++ ){

```

```

        for(unsigned k=0; k<m.size(3); k++ )
            cout << m[i][j][k] << ' ';
        cout << endl;
    }
    cout << "-----" << endl;
}

void test3a()
{
    Matrica<int,3,ProveraIndeksa> m(4,5,6);
    for(unsigned i=0;i<m.size(1);i++){
        Matrica<int,2,ProveraIndeksa> m2(5,6);
        for(unsigned k=0;k<m2.size(1);k++)
            for(unsigned j=0; j<m2.size(2); j++ )
                m2[k][j] = (i+1)*1000 + k*100 + j;
        m[i] = m2;
    }

    for(unsigned i=0;i<m.size(1);i++){
        for(unsigned j=0; j<m.size(2); j++ ){
            for(unsigned k=0; k<m.size(3); k++ )
                cout << m[i][j][k] << ' ';
            cout << endl;
        }
        cout << "-----" << endl;
    }
}

int main()
{
    try {
        test2();
        test3();
        test3a();
    }catch( exception& e ){
        cerr << "*** GRESKA: " << e.what() << endl;
    }

    return 0;
}

```

p79.matrica.cpp

```

#include <vector>
#include <iostream>
#include <stdexcept>

using namespace std;

// Primer sa efikasnom organizacijom memorije

```

```

// Matrica je niz elemenata sa slozenim indeksiranjem

//-----
// Politike provere indeksa
//-----
struct SaProveromIndeksa {
    static void Provera( int indeks, int velicina ) {
        if( indeks >= velicina )
            throw new out_of_range("Indeks van opsega!");
    }
};

struct BezProvereIndeksa {
    static void Provera( int indeks, int velicina ){}
};

//-----
// Struktura svih matrica je ista
//-----
template<class T,unsigned Dim,class ProveravacIndeksa>
class MatricaStructBase
{
public:
    typedef T tElement;

    static unsigned Dimenzija()
        { return Dim; }

    void PostaviVelicinu( unsigned* dimenzije )
    {
        _Velicina.clear();
        _Podvelicina.clear();
        unsigned n = 1;
        for( unsigned i=0; i<Dim; i++ ){
            _Podvelicina.push_back(n);
            _Velicina.push_back(dimenzije[i]);
            n *= dimenzije[i];
        }
        _Elementi.resize(n);
    }

    unsigned Velicina( unsigned n ) const
        { return _Velicina[n]; }

    unsigned RelativniIndeks( unsigned dim, unsigned i )
    {
        ProveravacIndeksa::Provera( i, _Velicina[dim] );
        return i * _Podvelicina[dim];
    }

    tElement& Element( unsigned i )
        { return _Elementi[i]; }
};

```

```

protected:
    vector< tElement >   _Elementi;      // elementi matrice
    vector< unsigned >   _Velicina;     // koliki je raspon kog indeksa
    vector< unsigned >   _Podvelicina;  // koliko ima elemenata podmatrica (*this)
[0], (*this)[0][1], (*this)[0][1][2],...
};

//-----
// Referenca na podmatricu
//-----
template<class tMatrica, unsigned Dim>
class ReferencaPodmatrice
{
public:
    ReferencaPodmatrice( tMatrica& mat, unsigned i )
        : _Matrica( mat ), _RelativniIndeks( i )
        {}

    ReferencaPodmatrice<tMatrica,Dim-1> operator[]( unsigned i )
    {
        unsigned indeks = _RelativniIndeks + _Matrica.RelativniIndeks(
tMatrica::Dimenzija() - Dim, i );
        return ReferencaPodmatrice<tMatrica,Dim-1>( _Matrica, indeks );
    }

protected:
    tMatrica&   _Matrica;
    unsigned   _RelativniIndeks;
};

template<class tMatrica>
class ReferencaPodmatrice<tMatrica,1>
{
public:
    ReferencaPodmatrice( tMatrica& mat, unsigned i )
        : _Matrica( mat ), _RelativniIndeks( i )
        {}

    typename tMatrica::tElement& operator[]( unsigned i )
    {
        unsigned indeks = _RelativniIndeks + _Matrica.RelativniIndeks(
tMatrica::Dimenzija() - 1, i );
        return _Matrica.Element( indeks );
    }

protected:
    tMatrica&   _Matrica;
    unsigned   _RelativniIndeks;
};

```

```

//-----
// Univerzalna matrica sa dim dimenzija
//-----
template<class tElement,unsigned Dim,class ProveravacIndeksa=BezProvereIndeksa>
class Matrica : public MatricaStructBase< tElement,Dim,ProveravacIndeksa >
{
public:
    Matrica()
        {}

    Matrica( unsigned* dimenzije )
        { MatricaStructBase< tElement,Dim,ProveravacIndeksa >::PostaviVelicinu(
dimenzije ); }

    ReferencaPodmatrice<Matrica,Dim-1> operator[] ( unsigned i )
    {
        unsigned indeks = MatricaStructBase< tElement,Dim,ProveravacIndeksa
>::RelativniIndeks( 0, i );
        return ReferencaPodmatrice<Matrica,Dim-1>( *this, indeks );
    }
};

//-----
// Primeri
//-----
void test2()
{
    unsigned dim[] = {2,5};
    Matrica<int,2,SaProveromIndeksa> m(dim);

    for( unsigned i=0; i<m.Velicina(0); i++ )
        for( unsigned j=0; j<m.Velicina(1); j++ )
            m[i][j] = i*10 + j;

    for( unsigned i=0; i<m.Velicina(0); i++ ){
        for( unsigned j=0; j<m.Velicina(1); j++ )
            cout << m[i][j] << ' ';
        cout << endl;
    }
}

void test3()
{
    unsigned dim[] = {2,5,7};
    Matrica<int,3,SaProveromIndeksa> m(dim);

    for( unsigned i=0; i<m.Velicina(0); i++ )
        for( unsigned j=0; j<m.Velicina(1); j++ )
            for( unsigned k=0; k<m.Velicina(2); k++ )
                m[i][j][k] = i*100 + j*10 + k;

    for( unsigned i=0; i<m.Velicina(0); i++ ){
        for( unsigned j=0; j<m.Velicina(1); j++ ){
            for( unsigned k=0; k<m.Velicina(2); k++ )

```

```

        cout << m[i][j][k] << ' ';
        cout << endl;
    }
    cout << "-----" << endl;
}
}

void test4()
{
    unsigned dim[] = {2,5,7,2};
    Matrica<int,4,SaProveromIndeksa> m(dim);

    for( unsigned i=0; i<m.Velicina(0); i++ )
        for( unsigned j=0; j<m.Velicina(1); j++ )
            for( unsigned k=0; k<m.Velicina(2); k++ )
                for( unsigned l=0; l<m.Velicina(3); l++ )
                    m[i][j][k][l] = i*1000 + j*100 + k*10 + l;

    for( unsigned i=0; i<m.Velicina(0); i++ ){
        for( unsigned j=0; j<m.Velicina(1); j++ ){
            for( unsigned k=0; k<m.Velicina(2); k++ ){
                for( unsigned l=0; l<m.Velicina(3); l++ )
                    cout << m[i][j][k][l] << ' ';
                cout << endl;
            }
            cout << "-----" << endl;
        }
        cout << "======" << endl;
    }
}

int main()
{
    test2();
    cout << endl;

    test3();
    cout << endl;

    test4();

    return 0;
}

```